

**Math 231 CALCULUS 2- Santilli**

**Worksheet B –Rotation of Axes.**

1.)  $xy + 1 = 0$

Answer:  
 $\frac{(y')^2}{2} - \frac{(x')^2}{2} = 1, \theta = 45^\circ$

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2.)  $x^2 - 10xy + y^2 + 1 = 0$

Answer:  
 $\frac{(x')^2}{1/4} - \frac{(y')^2}{1/6} = 1, \theta = 45^\circ$

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3.)  $xy - 2y - 4x = 0$

Answer:  
 $\frac{(x' - 3\sqrt{2})^2}{16} - \frac{(y' - \sqrt{2})^2}{16} = 1, \theta = 45^\circ$

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4.)  $5x^2 - 2xy + 5y^2 - 12 = 0$

Answer:  
 $\frac{(x')^2}{3} + \frac{(y')^2}{2} = 1, \theta = 45^\circ$

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5.)  $3x^2 - 2\sqrt{3}xy + y^2 + 2x + 2\sqrt{3}y = 0$

Answer:  
 $x' = -(y')^2, \theta = 60^\circ$

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6.)  $9x^2 + 24xy + 16y^2 + 90x - 130y = 0$

Answer:  
 $y' = \frac{(x')^2}{6} - \frac{x'}{3}, \theta = 53.13^\circ$