

For review use the 4-step process worksheet, the domain quizzes done in class, the transformation review and the following:

Find the domain of the following functions:

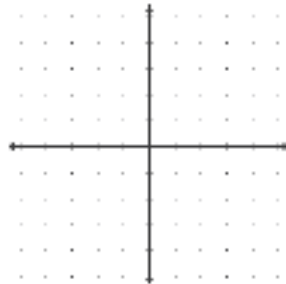
1) $f(x) = x^2 + 6$

2) $h(x) = \frac{x - 4}{x^3 - 36x}$

3) $f(x) = \sqrt{18 - x}$

Graph the function, and find the following:

4)
$$f(x) = \begin{cases} -2x - 3 & \text{if } x \leq -2 \\ x & \text{if } -2 < x \leq 1 \\ x^2 & \text{if } x > 1 \end{cases}$$

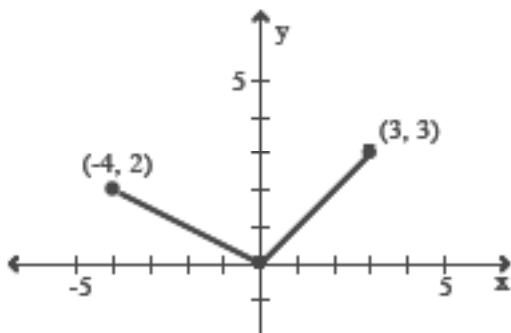


- a) Find $f(0)$
 $f(2)$
 $f(3)$

- b) Find Domain:
Range:

- c) x-Intercept(s)
y-Intercept

5)



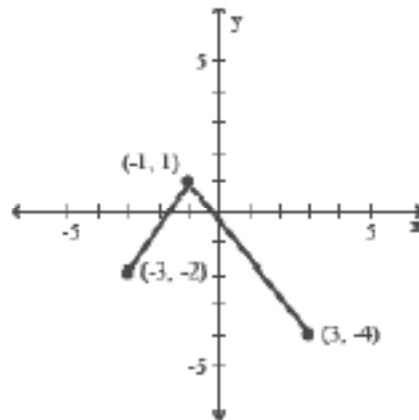
Write a definition for this function:

$$f(x) = \begin{cases} \underline{\hspace{2cm}} & \text{if } \underline{\hspace{2cm}} \\ \underline{\hspace{2cm}} & \text{if } \underline{\hspace{2cm}} \end{cases}$$

6. Given: $f(x) = \frac{x^2 - 4}{x - 8}$ Find the following:

- $f(-1)$
- x if $f(x) = \frac{1}{2}$
- the x -intercept(s)
- the y -intercept

7. The graph of a function f is illustrated below. Use the graph of f to graph the following new function: $F(x) = -\frac{1}{2}f(x+2) + 1$



8. List the transformation of $f(x) = -2\sqrt{-3x} - 4$

0: Basic Function

- 1:
- 2:
- 3:
- 4:
- 5:

9. Using $y = \sqrt[3]{x}$ as the basic function, write a function who has the following transformation:

- 1: left 3
- 2: Vertical stretch factor of 3
- 3: Reflect the x -axis
- 4: Up 2

10. Using the "4-step process" or some similar process and: $f(x) = 2x^2 - 3x$

Find: $\frac{f(x+h) - f(x)}{h}$

For review use the 4-step process worksheet, the domain quizzes done in class, the transformation review and the following:

Find the domain of the following functions:

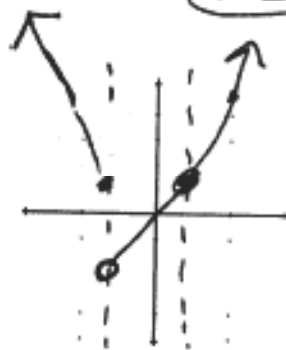
1) $f(x) = x^2 + 6 \Rightarrow \mathbb{R}$, no denominator - no radical

2) $h(x) = \frac{x-1}{x^3-36x}$
 Denominator $\neq 0$
 $x^3 - 36x \neq 0$
 $x(x^2 - 36) \neq 0$
 $x(x-6)(x+6) \neq 0$
 $x \neq 0, x \neq 6, x \neq -6$

3) $f(x) = \sqrt{18-x}$
 Radicand ≥ 0
 $18-x \geq 0$
 $-x \geq -18$
 $x \leq 18$

Graph the function, and find the following:

4) $f(x) = \begin{cases} -2x-3 & \text{if } x \leq -2 \\ x & \text{if } -2 < x \leq 1 \\ x^2 & \text{if } x > 1 \end{cases}$
 (Note: $x=0$ and $x=3$ are marked on the graph)



① $x \leq -2$

x	-2x-3
-2	1
-3	3

 Solid

② $-2 < x \leq 1$

x	x
-2	-2
1	1

 Open at -2, Solid at 1

③ $x > 1$

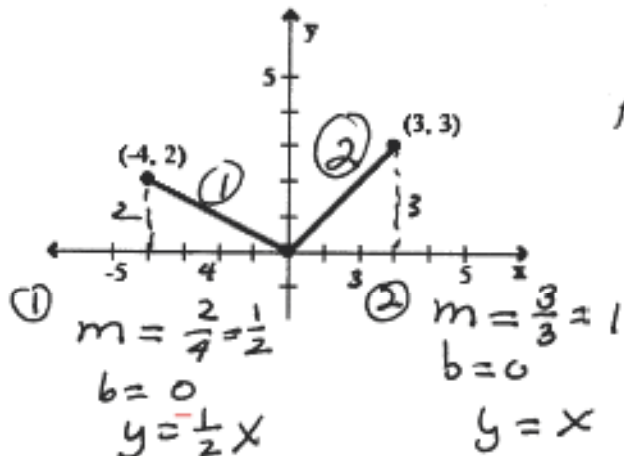
x	x ²
2	4
3	9
1	1

a) Find $f(0) = 0$
 $f(2) = 2^2 = 4$
 $f(3) = 3^2 = 9$

b) Find Domain: \mathbb{R}
 Range: $(-2, \infty)$

c) x-Intercept(s): $(0, 0)$
 y-Intercept: $(0, 0)$

5)



Write a definition for this function:

$$f(x) = \begin{cases} \frac{-1}{2}x & \text{if } -4 \leq x < 0 \\ x & \text{if } 0 \leq x \leq 3 \end{cases}$$

6. Given: $f(x) = \frac{x^2 - 4}{x - 8}$ Find the following:

a) $f(-1) = \frac{(-1)^2 - 4}{-1 - 8} = \frac{1 - 4}{-9} = \frac{-3}{-9} = \frac{1}{3}$

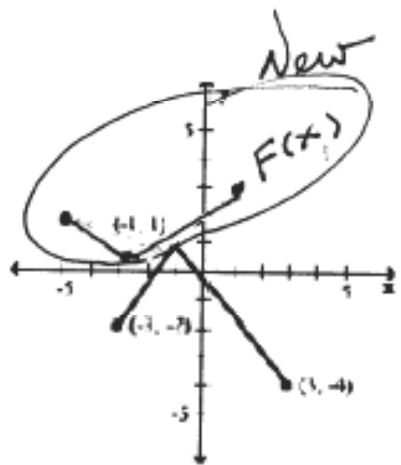
b) x if $f(x) = \frac{1}{2}$ $\frac{1}{2} = \frac{x^2 - 4}{x - 8} \Rightarrow 2(x^2 - 4) = x - 8$
 $2x^2 - 8 = x - 8$
 $2x^2 = x$
 $2x^2 - x = 0$
 $x(2x - 1) = 0$
 $x = 0$ or $x = \frac{1}{2}$

c) the x-intercept(s) $y = 0$ $x^2 - 4 = 0$ $(x - 2)(x + 2) = 0$ $(2, 0)$ $(-2, 0)$

d) the y-intercept $x = 0$ $y = \frac{-4}{-8} = \frac{1}{2}$ $(0, \frac{1}{2})$

7. The graph of a function f is illustrated below. Use the graph of f to graph the following new function: $F(x) = -\frac{1}{2}f(x-2) + 1$

- List:
- ① left + 2
 - ② Reflect x-axis
 - ③ V. Shrink factor $\frac{1}{2}$
 - ④ up 1



$+(-2)$	x	y	$\frac{1}{2}$	$+1$
-5	-3	-2	1	2
-3	-1	1	$-\frac{1}{2}$	$\frac{1}{2}$
+1	3	-4	2	3

8. List the transformation of $f(x) = -2\sqrt{-3x} - 4$

- 0: Basic Function
- 1: Reflect y-axis
- 2: H. Shrink factor $\frac{1}{3}$
- 3: reflect x-axis
- 4: v. stretch factor 2
- 5: down 4

9. Using $y = \sqrt[3]{x}$ as the basic function, write a function who has the following transformation:

- 1: left 3 $\sqrt[3]{(x + 3)}$
- 2: Vertical stretch factor of 3 $3\sqrt[3]{x + 3}$
- 3: Reflect the x-axis $-3\sqrt[3]{x + 3}$
- 4: Up 2 $-3\sqrt[3]{x + 3} + 2$

$y = -3\sqrt[3]{x + 3} + 2$

$$\begin{aligned}\textcircled{1} \quad f(x+h) &= 2(x+h)^2 - 3(x+h) \\ &= 2(x^2 + 2xh + h^2) - 3x - 3h \\ &= 2x^2 + 4xh + 2h^2 - 3x - 3h\end{aligned}$$

$$\textcircled{2} \quad f(x) = 2x^2 - 3x$$

$$\begin{aligned}\textcircled{3} \quad f(x+h) - f(x) &= 2x^2 + 4xh + 2h^2 - 3x - 3h - (2x^2 - 3x) \\ &= \cancel{2x^2} + 4xh + \cancel{2h^2} - \cancel{3x} - 3h - \cancel{2x^2} + \cancel{3x} \\ &= 4xh + 2h^2 - 3h\end{aligned}$$

$$\begin{aligned}\textcircled{4} \quad \frac{f(x+h) - f(x)}{h} &= \frac{4xh + 2h^2 - 3h}{h} \\ &= \frac{\cancel{h}(4x + 2h - 3)}{\cancel{h}} \\ &= \boxed{4x + 2h - 3}\end{aligned}$$